Introduction to Matlab (Code)

intro.m

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%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% Introduction to Matlab
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% (1) Basics

% The symbol "%" is used to indicate a comment (for the remainder of
% the line).

% When writing a long Matlab statement that becomes to long for a
% single line use "..." at the end of the line to continue on the next
% line.  E.g.

A = [1, 2; ...
     3, 4];

% A semicolon at the end of a statement means that Matlab will not
% display the result of the evaluated statement. If the ";" is omitted
% then Matlab will display the result.  This is also useful for
% printing the value of variables, e.g.

A

% Matlab's command line is a little like a standard shell:
% - Use the up arrow to recall commands without retyping them (and
%   down arrow to go forward in the command history).
% - C-a moves to beginning of line (C-e for end), C-f moves forward a
%   character and C-b moves back (equivalent to the left and right
%   arrow keys), C-d deletes a character, C-k deletes the rest of the
%   line to the right of the cursor, C-p goes back through the
%   command history and C-n goes forward (equivalent to up and down
%   arrows), Tab tries to complete a command.

% Simple debugging:
% If the command "dbstop if error" is issued before running a script
% or a function that causes a run-time error, the execution will stop
% at the point where the error occurred. Very useful for tracking down
% errors.



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% (2) Basic types in Matlab

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% (A) The basic types in Matlab are scalars (usually double-precision
% floating point), vectors, and matrices:

A = [1 2; 3 4];              % Creates a 2x2 matrix
B = [1,2; 3,4];              % The simplest way to create a matrix is
                             % to list its entries in square brackets.
                             % The ";" symbol separates rows;
                             % the (optional) "," separates columns.

N = 5                        % A scalar
v = [1 0 0]                  % A row vector
v = [1; 2; 3]                % A column vector
v = v'                       % Transpose a vector (row to column or
                             %   column to row)
v = 1:.5:3                   % A vector filled in a specified range:
v = pi*[-4:4]/4              %   [start:stepsize:end]
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                               %   (brackets are optional)
v = []                         % Empty vector



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% (B) Creating special matrices: 1ST parameter is ROWS,
%   2ND parameter is COLS

m = zeros(2, 3)                % Creates a 2x3 matrix of zeros
v = ones(1, 3)                 % Creates a 1x3 matrix (row vector) of ones
m = eye(3)                     % Identity matrix (3x3)
v = rand(3, 1)                 % Randomly filled 3x1 matrix (column
                               % vector); see also randn

                               % But watch out:
m = zeros(3)                   % Creates a 3x3 matrix (!) of zeros



%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% (C) Indexing vectors and matrices.
% Warning: Indices always start at 1 and *NOT* at 0!

v = [1 2 3];
v(3)                           % Access a vector element


m = [1 2 3 4; 5 7 8 8; 9 10 11 12; 13 14 15 16]
m(1, 3)                        % Access a matrix element
                               %       matrix(ROW #, COLUMN #)
m(2, :)                        % Access a whole matrix row (2nd row)
m(:, 1)                        % Access a whole matrix column (1st column)

m(1, 1:3)                      % Access elements 1 through 3 of the 1st row
m(2:3, 2)                      % Access elements 2 through 3 of the
                               %   2nd column
m(2:end, 3)                    % Keyword "end" accesses the remainder of a
                               %   column or row

m = [1 2 3; 4 5 6]
size(m)                        % Returns the size of a matrix
size(m, 1)                     % Number of rows
size(m, 2)                     % Number of columns

m1 = zeros(size(m))            % Create a new matrix with the size of m

who                            % List variables in workspace
whos                           % List variables w/ info about size, type, etc.



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% (3) Simple operations on vectors and matrices

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% (A) Element-wise operations:

% These operations are done "element by element".  If two
% vectors/matrices are to be added, subtracted, or element-wise
% multiplied or divided, they must have the same size.

a = [1 2 3 4]';                % A column vector
2 * a                          % Scalar multiplication
a / 4                          % Scalar division
b = [5 6 7 8]';                % Another column vector
a + b                          % Vector addition
a - b                          % Vector subtraction
a .^ 2                         % Element-wise squaring (note the ".")
a .* b                         % Element-wise multiplication (note the ".")
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a ./ b                          % Element-wise division (note the ".")

log([1 2 3 4])                  % Element-wise logarithm
round([1.5 2; 2.2 3.1])         % Element-wise rounding to nearest integer

% Other element-wise arithmetic operations include e.g. :
%   floor, ceil, ...


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% (B) Vector Operations
% Built-in Matlab functions that operate on vectors

a = [1 4 6 3]                   % A row vector
sum(a)                          % Sum of vector elements
mean(a)                         % Mean of vector elements
var(a)                          % Variance of elements
std(a)                          % Standard deviation
max(a)                          % Maximum
min(a)                          % Minimum

% If a matrix is given, then these functions will operate on each column
%   of the matrix and return a row vector as result
a = [1 2 3; 4 5 6]              % A matrix
mean(a)                         % Mean of each column
max(a)                          % Max of each column
max(max(a))                     % Obtaining the max of a matrix
mean(a, 2)                      % Mean of each row (second argument specifies
                                %   dimension along which operation is taken)


[1 2 3] * [4 5 6]'              % 1x3 row vector times a 3x1 column vector
                                %   results in a scalar.  Known as dot product
                                %   or inner product.  Note the absence of "."

[1 2 3]' * [4 5 6]              % 3x1 column vector times a 1x3 row vector
                                %   results in a 3x3 matrix.  Known as outer
                                %   product.  Note the absence of "."



%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% (C) Matrix Operations:

a = rand(3,2)                   % A 3x2 matrix
b = rand(2,4)                   % A 2x4 matrix
c = a * b                       % Matrix product results in a 3x4 matrix

a = [1 2; 3 4; 5 6];            % A 3x2 matrix
b = [5 6 7];                    % A 1x3 row vector
b * a                           % Vector-matrix product results in
                                %   a 1x2 row vector
c = [8; 9];                     % A 2x1 column vector
a * c                           % Matrix-vector product results in
                                %   a 3x1 column vector

a = [1 3 2; 6 5 4; 7 8 9];      % A 3x3 matrix
inv(a)                          % Matrix inverse of a
eig(a)                          % Vector of eigenvalues of a
[V, D] = eig(a)                 % D matrix with eigenvalues on diagonal;
                                %   V matrix of eigenvectors
                                %   Example for multiple return values!
[U, S, V] = svd(a)              % Singular value decomposition of a.
                                %   a = U * S * V', singular values are
                                %   stored in S

% Other matrix operations: det, norm, rank, ...


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```matlab
% (D) Reshaping and assembling matrices:

a = [1 2; 3 4; 5 6];          % A 3x2 matrix
b = a(:)                      % Make 6x1 column vector by stacking
                              %   up columns of a
sum(a(:))                     % Useful:  sum of all elements

a = reshape(b, 2, 3)          % Make 2x3 matrix out of vector
                              %   elements (column-wise)

a = [1 2]; b = [3 4];         % Two row vectors
c = [a b]                     % Horizontal concatenation (see horzcat)

a = [1; 2; 3];                % Column vector
c = [a; 4]                    % Vertical concatenation (see vertcat)

a = [eye(3) rand(3)]          % Concatenation for matrices
b = [eye(3); ones(1, 3)]

b = repmat(5, 3, 2)           % Create a 3x2 matrix of fives
b = repmat([1 2; 3 4], 1, 2) % Replicate the 2x2 matrix twice in
                              %   column direction; makes 2x4 matrix
b = diag([1 2 3])             % Create 3x3 diagonal matrix with given
                              %   diagonal elements



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% (4) Control statements & vectorization

% Syntax of control flow statements:
%
% for VARIABLE = EXPR
%     STATEMENT
%      ...
%     STATEMENT
% end
%
%   EXPR is a vector here, e.g. 1:10 or -1:0.5:1 or [1 4 7]
%
%
% while EXPRESSION
%     STATEMENTS
% end
%
% if EXPRESSION
%     STATEMENTS
% elseif EXPRESSION
%     STATEMENTS
% else
%     STATEMENTS
% end
%
%   (elseif and else clauses are optional, the "end" is required)
%
%   EXPRESSIONs are usually made of relational clauses, e.g. a < b
%   The operators are <, >, <=, >=, ==, ~=  (almost like in C(++))

% Warning:
%   Loops run very slowly in Matlab, because of interpretation overhead.
%   This has gotten somewhat better in version 6.5, but you should
%   nevertheless try to avoid them by "vectorizing" the computation,
%   i.e. by rewriting the code in form of matrix operations.  This is
%   illustrated in some examples below.

% Examples:
for i=1:2:7                   % Loop from 1 to 7 in steps of 2
  i                           % Print i
end
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for i=[5 13 -1]                 % Loop over given vector
  if (i > 10)                   % Sample if statement
    disp('Larger than 10')      % Print given string
  elseif i < 0                  % Parentheses are optional
    disp('Negative value')
  else
    disp('Something else')
  end
end


% Here is another example: given an mxn matrix A and a 1xn
% vector v, we want to subtract v from every row of A.

m = 50; n = 10; A = ones(m, n); v = 2 * rand(1, n);
%
% Implementation using loops:
for i=1:m
  A(i,:) = A(i,:) - v;
end

% We can compute the same thing using only matrix operations
A = ones(m, n) - repmat(v, m, 1);   % This version of the code runs
                                    %   much faster!!!


% We can vectorize the computation even when loops contain
%   conditional statements.
%
% Example: given an mxn matrix A, create a matrix B of the same size
%   containing all zeros, and then copy into B the elements of A that
%   are greater than zero.

% Implementation using loops:
B = zeros(m,n);
for i=1:m
  for j=1:n
    if A(i,j)>0
      B(i,j) = A(i,j);
    end
  end
end

% All this can be computed w/o any loop!
B = zeros(m,n);
ind = find(A > 0);              % Find indices of positive elements of A
                                %   (see "help find" for more info)
B(ind) = A(ind);                % Copies into B only the elements of A
                                %   that are > 0



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%(5) Saving your work

save myfile                     % Saves all workspace variables into
                                %   file myfile.mat
save myfile a b                 % Saves only variables a and b

clear a b                       % Removes variables a and b from the
                                %   workspace
clear                           % Clears the entire workspace

load myfile                     % Loads variable(s) from myfile.mat



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%(6) Creating scripts or functions using m-files:
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% Matlab scripts are files with ".m" extension containing Matlab
% commands.  Variables in a script file are global and will change the
% value of variables of the same name in the environment of the current
% Matlab session.  A script with name "script1.m" can be invoked by
% typing "script1" in the command window.

% Functions are also m-files. The first line in a function file must be
% of this form:
% function [outarg_1, ..., outarg_m] = myfunction(inarg_1, ..., inarg_n)
%
% The function name should be the same as that of the file
% (i.e. function "myfunction" should be saved in file "myfunction.m").
% Have a look at myfunction.m and myotherfunction.m for examples.
%
% Functions are executed using local workspaces: there is no risk of
% conflicts with the variables in the main workspace. At the end of a
% function execution only the output arguments will be visible in the
% main workspace.

a = [1 2 3 4];                  % Global variable a
b = myfunction(2 * a)           % Call myfunction which has local
                                %   variable a
a                               % Global variable a is unchanged

[c, d] = ...
  myotherfunction(a, b)         % Call myotherfunction with two return
                                % values


%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%(7) Plotting

x = [0 1 2 3 4];                % Basic plotting
plot(x);                        % Plot x versus its index values
pause                           % Wait for key press
plot(x, 2*x);                   % Plot 2*x versus x
axis([0 8 0 8]);                % Adjust visible rectangle

figure;                         % Open new figure
x = pi*[-24:24]/24;
plot(x, sin(x));
xlabel('radians');              % Assign label for x-axis
ylabel('sin value');            % Assign label for y-axis
title('dummy');                 % Assign plot title

figure;
subplot(1, 2, 1);               % Multiple functions in separate graphs
plot(x, sin(x));                %   (see "help subplot")
axis square;                    % Make visible area square
subplot(1, 2, 2);
plot(x, 2*cos(x));
axis square;

figure;
plot(x, sin(x));
hold on;                        % Multiple functions in single graph
plot(x, 2*cos(x), '--');        % '--' chooses different line pattern
legend('sin', 'cos');           % Assigns names to each plot
hold off;                       % Stop putting multiple figures in current
                                %   graph

figure;                         % Matrices vs. images
m = rand(64,64);
imagesc(m)                      % Plot matrix as image
colormap gray;                  % Choose gray level colormap
axis image;                     % Show pixel coordinates as axes
axis off;                       % Remove axes
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%(8) Working with (gray level) images

I = imread('cit.png');          % Read a PNG image

figure
imagesc(I)                     % Display it as gray level image
colormap gray;

colorbar                       % Turn on color bar on the side
pixval                         % Display pixel values interactively
truesize                       % Display at resolution of one screen
                               %   pixel per image pixel
truesize(2*size(I))            % Display at resolution of two screen
                               %   pixels per image pixel

I2 = imresize(I, 0.5, 'bil'); % Resize to 50% using bilinear
                               %   interpolation
I3 = imrotate(I2, 45, ...      % Rotate 45 degrees and crop to
              'bil', 'crop'); %   original size

I3 = double(I2);               % Convert from uint8 to double, to allow
                               %   math operations
imagesc(I3.^2)                 % Display squared image (pixel-wise)
imagesc(log(I3))               % Display log of image (pixel-wise)
I3 = uint8(I3);                % Convert back to uint8 for writing
imwrite(I3, 'test.png')        % Save image as PNG

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myfunction.m

```
function y = myfunction(x)
% Function of one argument with one return value

a = [-2 -1 0 1];               % Have a global variable of the same name
y = a + x;
```

myotherfunction.m

```
function [y, z] = myotherfunction(a, b)
% Function of two arguments with two return values

y = a + b;
z = a - b;
```

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