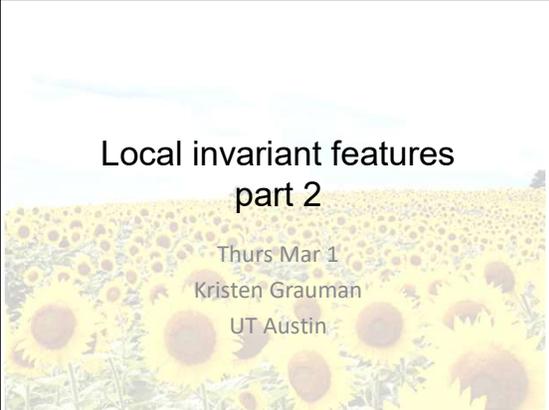


## Local invariant features part 2

Thurs Mar 1  
Kristen Grauman  
UT Austin



### Announcements

- Reminder - Midterm next Thursday Mar 8
  - Closed book
  - One 8.5x11" sheet of notes allowed (both sides)
  - Content up to and including Thurs 3/1 lecture
- Practice midterm handout today

### Important tool for multiple views: Local features



Multi-view matching relies on **local feature** correspondences.

How to *detect* which local features to match?  
How to *describe* the features we detect?

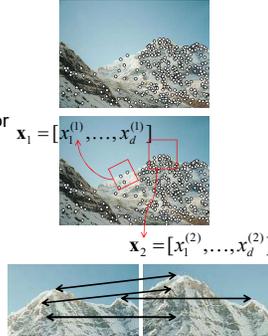
Slide credit: Kristen Grauman

### Outline

- **Last time:** Interest point detection
  - Harris corner detector
- **Today:**
  - Laplacian of Gaussian, automatic scale selection
  - Local descriptors for image patches
  - Matching sets of features

### Local features: main components

- 1) **Detection:** Identify the interest points
- 2) **Description:** Extract vector feature descriptor surrounding each interest point.
 
$$\mathbf{x}_1 = [x_1^{(1)}, \dots, x_d^{(1)}]$$
- 3) **Matching:** Determine correspondence between descriptors in two views
 
$$\mathbf{x}_2 = [x_1^{(2)}, \dots, x_d^{(2)}]$$

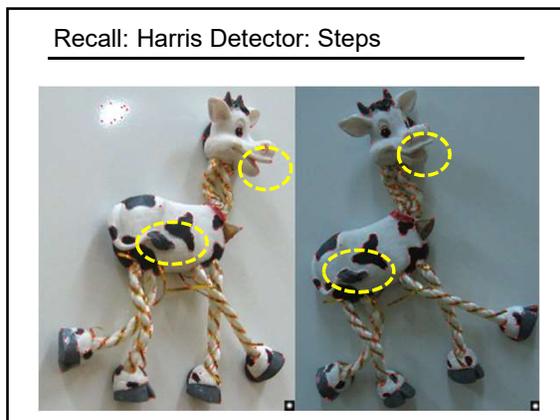
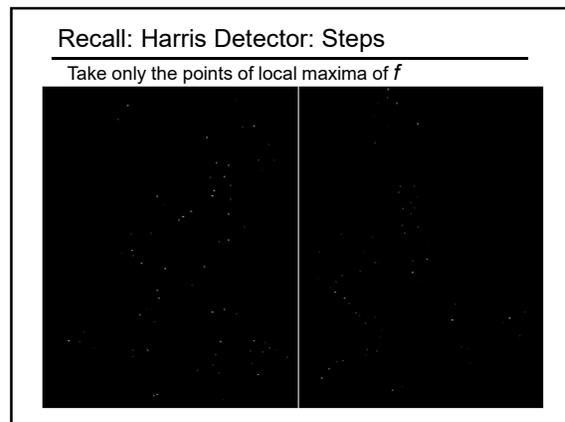
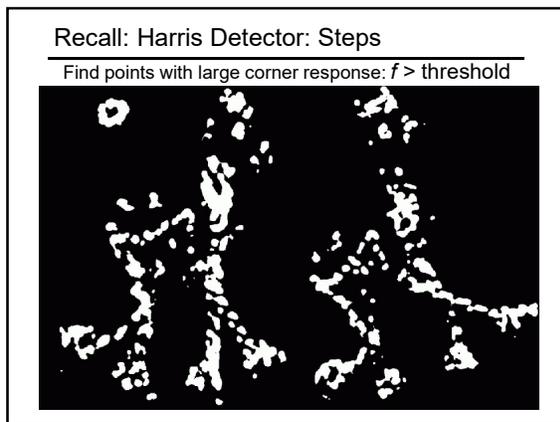
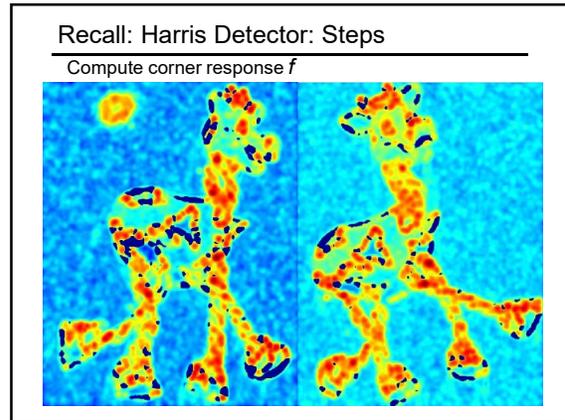
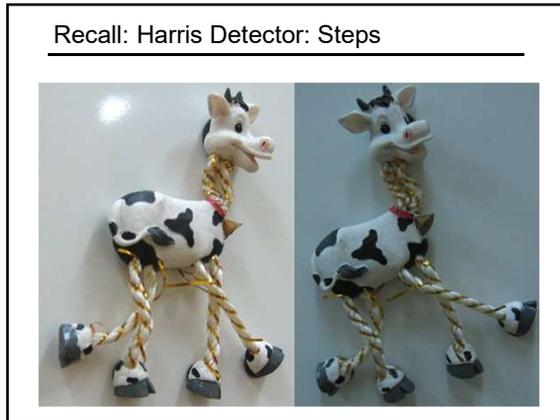


Slide credit: Kristen Grauman

### Recall: Harris corner detector

$$M = \sum w(x, y) \begin{bmatrix} I_x I_x & I_x I_y \\ I_x I_y & I_y I_y \end{bmatrix}$$

- 1) Compute  $M$  matrix for each image window to get their *cornerness* scores.
- 2) Find points whose surrounding window gave large corner response ( $f >$  threshold)
- 3) Take the points of local maxima, i.e., perform non-maximum suppression



- ### Review questions
- What properties should an interest operator have?
  - What will determine how many interest points a given image has?
  - What changes for Harris corner detections for in-plane or out-of-plane image rotations?

### Properties of the Harris corner detector

Rotation invariant? Yes

Scale invariant? No

All points will be classified as edges

Corner!

### Scale invariant interest points

How can we independently select interest points in each image, such that the detections are repeatable across different scales?

Slide credit: Kristen Grauman

### Automatic Scale Selection

How to find corresponding patch sizes, with only one image in hand?

K. Grauman, B. Leibe

### Automatic scale selection

**Intuition:**

- Find scale that gives local maxima of some function  $f$  in both position and scale.

### Automatic Scale Selection

- Function responses for increasing scale (scale signature)

K. Grauman, B. Leibe

### Automatic Scale Selection

- Function responses for increasing scale (scale signature)

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### Automatic Scale Selection

- Function responses for increasing scale (scale signature)

Left plot:  $f(U_{\dots} (x, \sigma))$  vs scale. Right plot:  $f(U_{\dots} (x', \sigma))$  vs scale.

K. Grauman, B. Leibe

### Automatic Scale Selection

- Function responses for increasing scale (scale signature)

Left plot:  $f(U_{\dots} (x, \sigma))$  vs scale. Right plot:  $f(U_{\dots} (x', \sigma))$  vs scale.

K. Grauman, B. Leibe

### Automatic Scale Selection

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### Automatic Scale Selection

- Function responses for increasing scale (scale signature)

Left plot:  $f(U_{\dots} (x, \sigma))$  vs scale. Right plot:  $f(U_{\dots} (x', \sigma))$  vs scale.

K. Grauman, B. Leibe

What can be the “signature” function?

### Blob detection in 2D

Laplacian of Gaussian: Circularly symmetric operator for blob detection in 2D

$$\nabla^2 g = \frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2}$$

### Blob detection in 2D: scale selection

Laplacian-of-Gaussian = "blob" detector  $\nabla^2 g = \frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2}$

Slide credit: Bastian Leibe

### Blob detection in 2D

We define the *characteristic scale* as the scale that produces peak of Laplacian response

Slide credit: Lana Lazebnik

### Example

Original image at ¼ the size

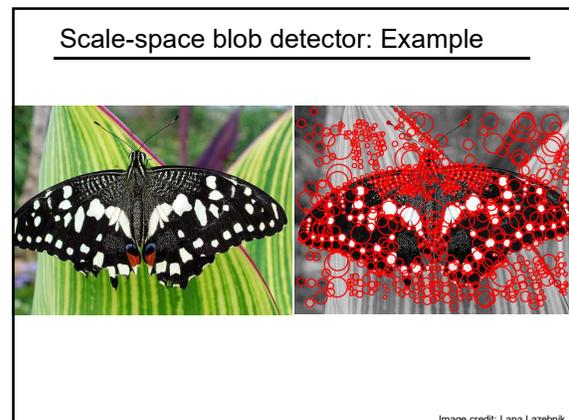
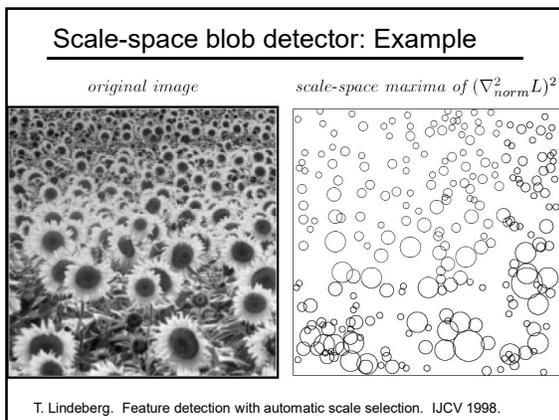
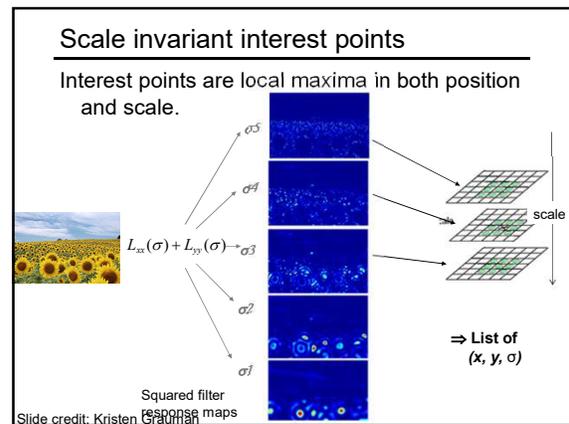
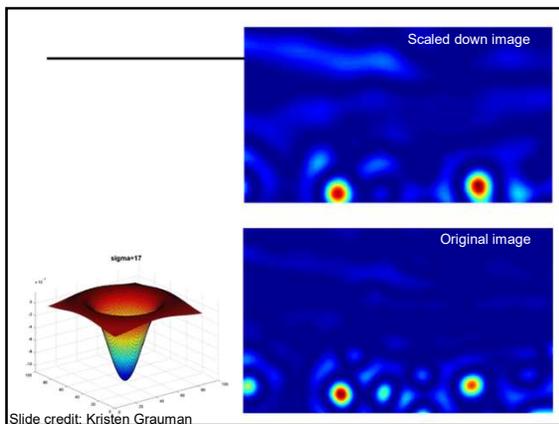
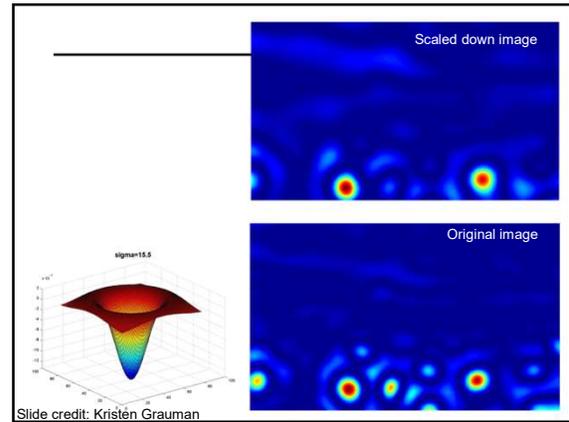
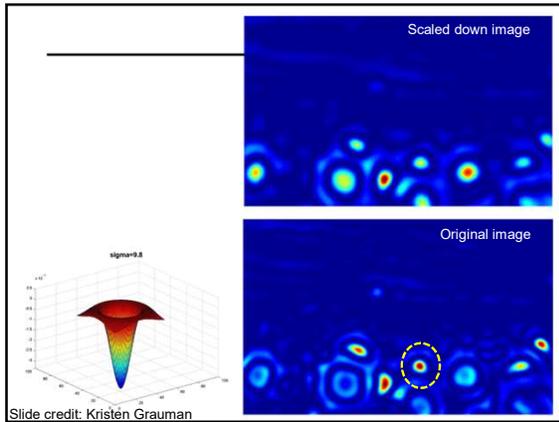
Slide credit: Kristen Grauman

Original image at ¼ the size

Slide credit: Kristen Grauman

Slide credit: Kristen Grauman

Slide credit: Kristen Grauman



### Technical detail

We can approximate the Laplacian with a difference of Gaussians; more efficient to implement.

$$L = \sigma^2 (G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma))$$

(Laplacian)

$$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$$

(Difference of Gaussians)

### Summary so far

- Desirable properties for local features for correspondence
- Basic matching pipeline
- Interest point detection
  - Harris corner detector
  - Laplacian of Gaussian, automatic scale selection

### Local features: main components

- 1) Detection: Identify the interest points
- 2) Description: Extract vector feature descriptor surrounding each interest point.
 
$$\mathbf{x}_1 = [x_1^{(1)}, \dots, x_d^{(1)}]$$

$$\mathbf{x}_2 = [x_1^{(2)}, \dots, x_d^{(2)}]$$
- 3) Matching: Determine correspondence between descriptors in two views

Slide credit: Kristen Grauman

### Geometric transformations

e.g. scale, translation, rotation

### Photometric transformations

Figure from T. Tuytelaars ECCV 2006 tutorial

### Raw patches as local descriptors

The simplest way to describe the neighborhood around an interest point is to write down the list of intensities to form a feature vector.

But this is very sensitive to even small shifts, rotations.

Figure: Andrew Zisserman

### Scale Invariant Feature Transform (SIFT) descriptor [Lowe 2004]

- Use histograms to bin pixels within sub-patches according to their orientation.

gradients

subdivided local patch

histogram per grid cell

Final descriptor = concatenation of all histograms, normalize

### Scale Invariant Feature Transform (SIFT) descriptor [Lowe 2004]

Interest points and their scales and orientations (random subset of 50)

SIFT descriptors

<http://www.vlfeat.org/overview/sift.html>

### Making descriptor rotation invariant

- Rotate patch according to its dominant gradient orientation
- This puts the patches into a canonical orientation.

Image from Matthew Brown

### SIFT descriptor [Lowe 2004]

- Extraordinarily robust matching technique
  - Can handle changes in viewpoint
    - Up to about 60 degree out of plane rotation
  - Can handle significant changes in illumination
    - Sometimes even day vs. night (below)
  - Fast and efficient—can run in real time
  - Lots of code available, e.g. <http://www.vlfeat.org/overview/sift.html>

Steve Seitz

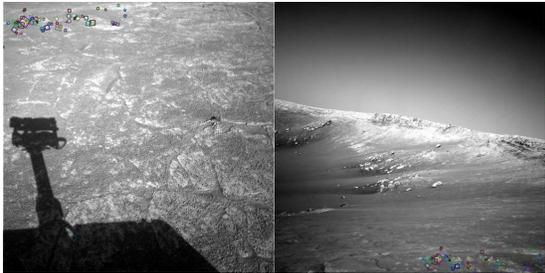
### SIFT properties

- Invariant to
  - Scale
  - Rotation
- Partially invariant to
  - Illumination changes
  - Camera viewpoint
  - Occlusion, clutter

### Example

NASA Mars Rover images

### Example



NASA Mars Rover images with SIFT feature matches  
Figure by Noah Snavely

### Local features: main components

- 1) Detection: Identify the interest points
- 2) Description: Extract vector feature descriptor surrounding each interest point.
- 3) Matching: Determine correspondence between descriptors in two views



Slide credit: Kristen Grauman

### Matching local features



Slide credit: Kristen Grauman

### Matching local features

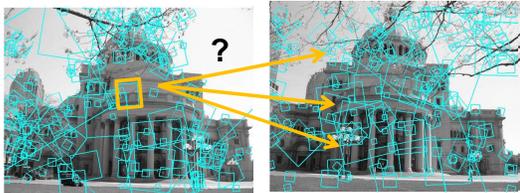


Image 1                      Image 2

To generate **candidate matches**, find patches that have the most similar appearance (e.g., lowest SSD)  
Simplest approach: compare them all, take the closest (or closest k, or within a thresholded distance)

Slide credit: Kristen Grauman

### Ambiguous matches

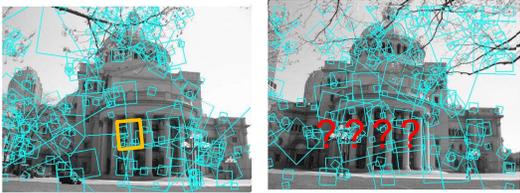


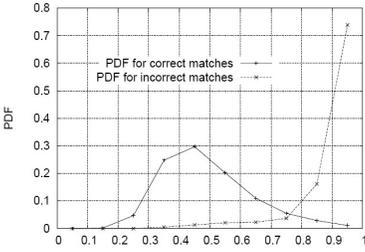
Image 1                      Image 2

At what SSD value do we have a good match?  
To add robustness to matching, consider **ratio** :  
dist to best match / dist to second best match  
If **low**, first match looks good.  
If **high**, could be **ambiguous match**.

Slide credit: Kristen Grauman

### Matching SIFT Descriptors

- Nearest neighbor (Euclidean distance)
- Threshold ratio of nearest to 2<sup>nd</sup> nearest descriptor



PDF

Ratio of distances (closest/next closest)

PDF for correct matches  
PDF for incorrect matches

Lowe IJCV 2004

### Scale Invariant Feature Transform (SIFT) descriptor [Lowe 2004]

Interest points and their scales and orientations (random subset of 50)

SIFT descriptors

<http://www.vlfeat.org/overview/sift.html>

### SIFT (preliminary) matches

img1

img2

img1

img2

<http://www.vlfeat.org/overview/sift.html>

### Value of local (invariant) features

- Complexity reduction via selection of distinctive points
- Describe images, objects, parts without requiring segmentation
  - Local character means robustness to clutter, occlusion
- Robustness: similar descriptors in spite of noise, blur, etc.

### Applications of local invariant features

- Wide baseline stereo
- Motion tracking
- Panoramas
- Mobile robot navigation
- 3D reconstruction
- Recognition
- ...

### Automatic mosaicing

Matthew Brown  
<http://matthewalunbrown.com/autostitch/autostitch.html>

### Wide baseline stereo

[Image from T. Tuytelaars ECCV 2006 tutorial]

