

Last time

- Feature-based alignment - 2D transformations
 - Affine fit
 - RANSAC











Source: L. Lazebnik









How many trials for RANSAC?						
To ensure good chance of finding true inliers, need sufficient number of trials, S.						
Let p be probability that any given match is valid						
Let P be to the total prob of success after S trials.						
Likelihood in one trial that all k random samples are						
inliers is p ^k	k	n	S			
Likelihood that all S trials will fa	~	٢	U			
1-P = (1-p ^k) ^S	3	0.5	35			
Required minimum number of to S = log(1-P) / log(1-p ^k)	6	0.6	97			
	6	0.5	293			
Kristen Grauman						



Last time: RANSAC for fitting a *model* (line)...

What about fitting a *transformation* (e.g., translation)?

RANSAC: General form

- RANSAC loop:
- 1. Randomly select a *seed group* on which to base transformation estimate (e.g., a group of matches)
- 2. Compute transformation from seed group
- 3. Find inliers to this transformation
- 4. If the number of inliers is sufficiently large, re-compute estimate of transformation on all of the inliers
- Keep the transformation with the largest number of inliers











Another example

Automatic scanned document rotater using Hough lines and RANSAC

https://www.youtube.com/watch?v=O0v9FAk43 kY

RANSAC pros and cons

- Pros
 - Simple and general
 - Applicable to many different problems
 - Often works well in practice
- Cons
 - · Parameters to tune
 - Doesn't work well for low inlier ratios (too many iterations, or can fail completely)
 - Can't always get a good initialization of the model based on the minimum number of samples

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RANSAC for estimating homography

RANSAC loop:

- 1. Select four feature pairs (at random)
- 2. Compute homography H
- 3. Compute *inliers* where $SSD(p_i) \in \varepsilon$
- 4. Keep largest set of inliers
- 5. Re-compute least-squares H estimate on all of the inliers

Slide credit: Steve Seit

Today

• Image mosaics

- Fitting a 2D transformation
- Affine, Homography
- 2D image warping
- Computing an image mosaic

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Image mosaics

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Recap: How to stitch together a panorama (a.k.a. mosaic)?

- Basic Procedure
 - Take a sequence of images from the same position
 Rotate the camera about its optical center
 - Compute transformation (homography) between second image and first using corresponding points.
 - Transform the second image to overlap with the first.

Source: Steve Seitz

- Blend the two together to create a mosaic.
- (If there are more images, repeat)

Summary: alignment & warping

- Write 2d transformations as matrix-vector multiplication (including translation when we use homogeneous coordinates)
- Perform image warping (forward, inverse)
- Fitting transformations: solve for unknown parameters given corresponding points from two views (affine, projective (homography)).
- **Mosaics**: uses homography and image warping to merge views taken from same center of projection.