

Image warping and stitching



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Announcements

- Midterm is Thursday
 - Covers all material up to and including last Thurs
 - Closed book, 1 sheet notes allowed
 - No coding, no Matlab

Last time

- Feature-based alignment
 - 2D transformations
 - Affine fit
 - RANSAC

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Robust feature-based alignment





Source: L. Lazebnik

Robust feature-based alignment





Extract features

Source: L. Lazebnik

Robust feature-based alignment



- Extract features
- Compute putative matches

Source: L. Lazebnik

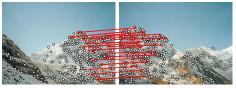
Robust feature-based alignment



- Extract features
- Compute putative matches
- · Loop:
 - Hypothesize transformation T (small group of putative matches that are related by T)

Source: L. Lazebnik

Robust feature-based alignment



- · Extract features
- Compute putative matches
- Loop:
 - Hypothesize transformation T (small group of putative matches that are related by T)
 - Verify transformation (search for other matches consistent with T)

Source: L. Lazebnik

Robust feature-based alignment



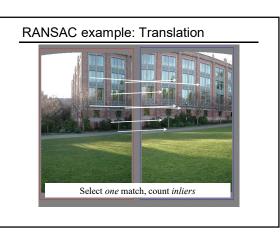
- Extract features
- Compute putative matches
- · Loop:
 - Hypothesize transformation T (small group of putative matches that are related by T)
 - Verify transformation (search for other matches consistent with T)

Source: L. Lazebnik

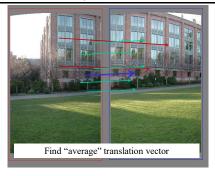
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RANSAC for line fitting example	
1. Randomly select minimal subset of points 2. Hypothesize a model 3. Compute error	
function 4. Select points consistent with model 5. Repeat hypothesize-and- verify loop	
Source: R. Raguram Lana Lazebnik	
Last time: RANSAC for fitting a model	
(line)	
What about fitting a <i>transformation</i> (e.g.,	
translation)?	
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RANSAC: General form	
RANSAC loop:	
Randomly select a seed group on which to base transformation estimate (e.g., a group of matches)	
Compute transformation from seed group	
3. Find <i>inliers</i> to this transformation	
If the number of inliers is sufficiently large, re-compute estimate of transformation on all of the inliers	
Keep the transformation with the largest number of inliers	

RANSAC example: Translation Putative matches Source: Rick Szeliski

RANSAC example: Translation Select one match, count inliers



RANSAC example: Translation



RANSAC pros and cons

- Pros
 - Simple and general
 - Applicable to many different problems
 - Often works well in practice
- Cons
 - · Parameters to tune
 - Doesn't work well for low inlier ratios (too many iterations, or can fail completely)
 - Can't always get a good initialization of the model based on the minimum number of samples



Today

- · Image mosaics
 - Fitting a 2D transformation
 - Affine, Homography
 - 2D image warping
 - Computing an image mosaic

Mosaics Image from 5.5 solz Obtain a wider angle view by combining multiple images.

Main questions					
•		Alignment: Given two images, what is the transformation between them?			
•	$\xrightarrow{T} \bullet \bullet \bullet \bullet$	Warping: Given a source image and a transformation, what does the transformed output look like?			

2D Affine Transformations $\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$ Affine transformations are combinations of ... • Linear transformations, and • Translations Parallel lines remain parallel

Projective Transformations

$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

Projective transformations:

- · Affine transformations, and
- Projective warps

Parallel lines do not necessarily remain parallel



2D transformation models

 Similarity (translation, scale, rotation)





• Projective (homography)



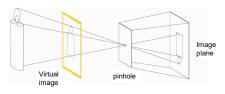
How to stitch together a panorama (a.k.a. mosaic)?

- · Basic Procedure
 - Take a sequence of images from the same position
 - Rotate the camera about its optical center
 - Compute transformation between second image and first
 - Transform the second image to overlap with the first
 - Blend the two together to create a mosaic
 - (If there are more images, repeat)
- ...but wait, why should this work at all?
 - What about the 3D geometry of the scene?
 - Why aren't we using it?

Source: Steve Seitz

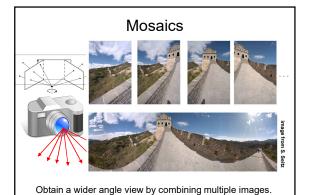
Pinhole camera

• Pinhole camera is a simple model to approximate imaging process, perspective **projection**.

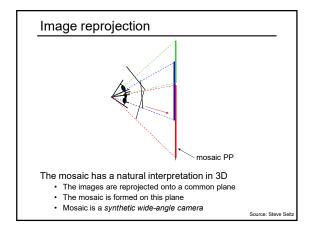


If we treat pinhole as a point, only one ray from any given point can enter the camera.

Fig from Forsyth and Ponce



Mosaics: generating synthetic views real synthetic camera camera Synthetic camera view as long as it has the same center of projection! Source: Alyosha Efros



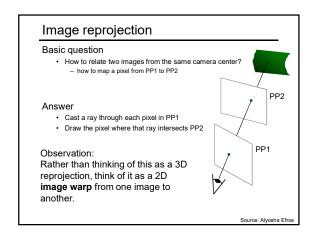
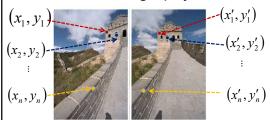


Image reprojection: Homo	graphy
A projective transform is a mapping be with the same center of projection rectangle should map to arbitrary quad parallel lines aren't but must preserve straight lines called Homography	,
$\begin{bmatrix} ux' \\ uy' \\ w \end{bmatrix} = \begin{bmatrix} * & * & * \\ * & * & * \\ * & * & * \end{bmatrix} \begin{bmatrix} x \\ y \\ f \end{bmatrix}$ \mathbf{p}^{2} \mathbf{H}	PP1 Source: Alyosha Efro

Homography



To compute the homography given pairs of corresponding points in the images, we need to set up an equation where the parameters of **H** are the unknowns...

Solving for homographies

$$\begin{bmatrix} wx' \\ wy' \\ w \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Can set scale factor i=1. So, there are 8 unknowns. Set up a system of linear equations:

where vector of unknowns $h = [a,b,c,d,e,f,g,h]^T$ Need at least 8 eqs, but the more the better...

Solve for h. If overconstrained, solve using least-squares:

$$\min \left\|Ah - b\right\|^2$$

>> help lmdivide

BOARD

Homography





$$= \left(\frac{wx'}{w}, \frac{wy'}{w}\right)$$
$$= \left(x', y'\right)$$

To **apply** a given homography **H**

- Compute p' = Hp (regular matrix multiply)
 Convert p' from homogeneous to image coordinates

$\lceil wx' \rceil$	*	*	*	$\lceil x \rceil$
wv' =	*	*	*	v
w	*	*	*	1
,	_		_	∟ 」

RANSAC for estimating homography

RANSAC loop:

- 1. Select four feature pairs (at random)
- 2. Compute homography H
- 3. Compute *inliers* where $SSD(p_i', Hp_i) \le \varepsilon$
- 4. Keep largest set of inliers
- 5. Re-compute least-squares H estimate on all of the inliers

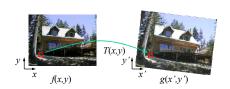


Slide credit: Steve Seit

Today

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 - Fitting a 2D transformation
 - Affine, Homography
 - 2D image warping
 - Computing an image mosaic

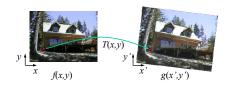
Image warping



Given a coordinate transform and a source image f(x,y), how do we compute a transformed image g(x',y') = f(T(x,y))?

Slide from Alyosha Efros, CMU

Forward warping

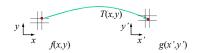


Send each pixel f(x,y) to its corresponding location (x',y') = T(x,y) in the second image

Q: what if pixel lands "between" two pixels?

Slide from Alyosha Efros, CMU

Forward warping



Send each pixel f(x,y) to its corresponding location (x',y') = T(x,y) in the second image

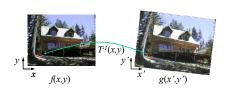
Q: what if pixel lands "between" two pixels?

A: distribute color among neighboring pixels (x',y')

- Known as "splatting"

Slide from Alyosha Efros, CMU

Inverse warping



Get each pixel g(x',y') from its corresponding location $(x,y) = T^{-1}(x',y')$ in the first image

Q: what if pixel comes from "between" two pixels?

Slide from Alyosha Efros, CMU

Inverse warping



Get each pixel g(x',y') from its corresponding location $(x,y) = T^{-1}(x',y')$ in the first image

Q: what if pixel comes from "between" two pixels?

A: Interpolate color value from neighbors

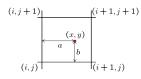
- nearest neighbor, bilinear...

>> help interp2

Bilinear interpolation

Sampling at f(x,y):

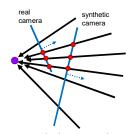
m Alyosha Efros, CMU



$$\begin{split} f(x,y) = & & (1-a)(1-b) \quad f[i,j] \\ & + a(1-b) \quad f[i+1,j] \\ & + ab \quad f[i+1,j+1] \\ & + (1-a)b \quad f[i,j+1] \end{split}$$

Slide from Alyosha Efros, CMU

Recall: generating synthetic views



Can generate any synthetic camera view as long as it has the same center of projection!

Source: Alyosha Efro

Recap: How to stitch together a panorama (a.k.a. mosaic)?

- · Basic Procedure
 - Take a sequence of images from the same position
 - Rotate the camera about its optical center
 - Compute transformation (homography) between second image and first using corresponding points.
 - Transform the second image to overlap with the first.
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 - (If there are more images, repeat)

Source: Steve Seitz

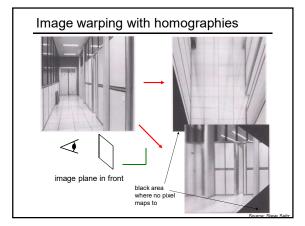
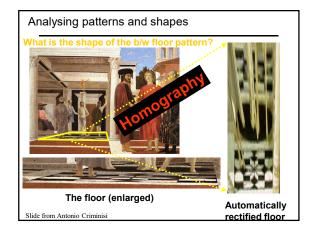
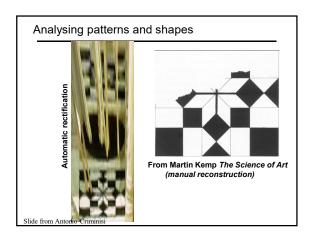
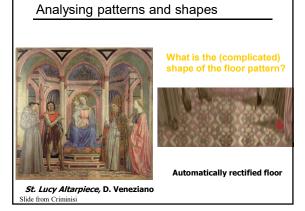
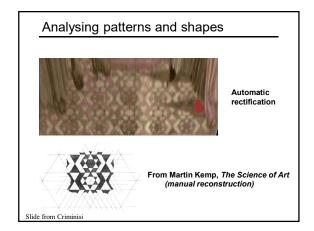


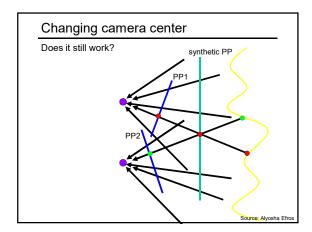
Image rectification

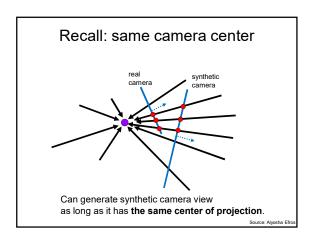












PP3 is a projection plane of both centers of projection, so we are OK! This is how big aerial photographs are made





Boundary extension

Wide-Angle Memories of Close-Up Scenes, Helene Intraub and Michael Richardson, Journal of Experimental Psychology: Learning, Memory, and Cognition, 1989, Vol. 15, No. 2, 179-187

Creating and Exploring a Large Photorealistic Virtual Space Josef Sivic, Biliana Kaneva, Antonio Torralba, Shai Avidan and William T. Freeman, Internet Vision Workshop, CVPR 2008. http://www.youtube.com/watch?v=E0rboU10PPc

Summary: alignment & warping

- Write 2d transformations as matrix-vector multiplication (including translation when we use homogeneous coordinates)
- Perform **image warping** (forward, inverse)
- **Fitting transformations**: solve for unknown parameters given corresponding points from two views (affine, projective (homography)).
- Mosaics: uses homography and image warping to merge views taken from same center of projection.